

SEMINARIO DI GEOMETRIA

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Politecnico di Torino,
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AULA SEMINARI

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On the smoothness of the Nori-Hilbert Scheme of 2 - Calabi Yau Algebras

Let A be a finitely generated k -algebra over an algebraically closed field of characteristic zero. Let R be a commutative k -algebra. The n -th Nori-Hilbert scheme of A is the scheme whose R -points parameterize cyclic A -module that locally free of rank n as R -module. If A is commutative this is the usual Hilbert scheme of n points on $\text{Spec}A$. An algebra is Calabi Yau of dimension d if the d -th shift functor in the derived category of finite dimensional (left) A -modules is a Serre functor. We give a sufficient condition for an irreducible component of the Nori - Hilbert scheme of A to be smooth when A is 2 - Calabi Yau.

As an application we prove that all Nori - Hilbert schemes of A are smooth when $A = k[G]$, where G is the fundamental group of a compact aspherical orientable complex surface of genus g and we recover the standard smoothness property of the Hilbert scheme of n -points of an irreducible smooth surface. Joint work with Federica Galluzzi